

national accelerator laboratory

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TRANSFER FUNCTION BETWEEN MAGNETIC FIELD AND EXCITATION CURRENT IN MAIN RING BENDING MAGNETS

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SUMMARY

The transfer function between the Fourier amplitudes of the central magnetic field and the excitation current has been calculated using equivalent magnetic circuit analysis. Reluctance effects, eddy currents in the laminations, eddy currents in the vacuum chamber, and eddy currents in the conductors are all included in the calculation. In addition, the impedance looking into the conductor terminals has been calculated. Results are presented for the B1 and B2 main ring bending magnets. Also included is the $\int B ds$ around the ring for the design distribution of B1 and B2 magnets.



MAGNETIC CIRCUIT

Figure 1 indicates the magnet cross section under consideration. Let b designate the half width of the pole, h the half-gap height, p the effective pole height, w the yoke width assumed the same in both the top and side yoke, and ℓ the average length of the flux path through the top and side yokes. The effective pole half width is taken to be $b+h$. Hence the flux density B_o in the top and side yoke is given approximately by

$$\int_0^{b+h} H_y(x, h) dx = wB_o. \quad (1)$$

Recognizing that the flux must be continuous across the boundary $y = h$, it is reasonable to let B in the pole vary with y according to

$$B(y) = \frac{1}{b} \int_0^b H_y(x, h) dx + \left[B_o - \frac{1}{b} \int_0^b H_y(x, h) dx \right] \cdot \frac{y-h}{p-h}. \quad (2)$$

Appendix I indicates that the effect of eddy currents in magnet laminations is to introduce a sheet current in the z -direction lining the coil window of total amount $\int i_I dl$ integrated over the mean path length where for

$$i_I = \frac{\lambda\delta}{8\pi\mu} \cdot \frac{\cosh \frac{\lambda\delta}{2} - 1}{\sinh \frac{\lambda\delta}{2}} B, \text{ (emu)} \quad (3)$$

where δ is the lamination thickness, μ the permeability of the iron and

$$\lambda^2 = 4\pi\mu j\omega. \quad (\text{emu}) \quad (4)$$

The conductivity of the iron is σ and ω is the angular frequency with which all magnetic and electrical field quantities are assumed to vary.

Appendix II indicates that eddy currents flowing in the vacuum chamber are represented by current sheets flowing in the z-direction of amount

$$i_C(x,y) = j\omega s U(x,y), \quad (\text{emu}) \quad (5)$$

where $U(x,y)$ is the flux function. The coordinates x and y are given values only at the location of the chamber which will be assumed rectangular of half width a and half height h . Surface conductivity of the vacuum chamber is designated by s .

One may complete the magnetic circuit description using the scalar potential function $V(x,y)$ corresponding to $U(x,y)$ and the notion of a mean flux path in the iron. Thus for $0 < x < a$ and (emu)

$$V(x,h) + \frac{1}{\mu} \int_h^p B(y) dy + \frac{\ell-p+h}{\mu} B_o = 2\pi NI - 4\pi \int_h^p i_I(y) dy \\ - 4\pi(\ell-p+h)i_I - 4\pi \int_x^a i_C(x,h) dx - 4\pi \int_0^h i_C(a,y) dy. \quad (6)$$

For $a < x < b + h$ the terms in i_C are dropped. Note that I is the excitation current and N the number of turns in the full gap. Note also that $i_I = i_I(p)$.

Appendix III gives the fields to be used in the region of the vacuum chamber. Outside the chamber the fields are obtained

approximately as follows. First $4\pi i_c(a, h)$ is added to the vertical field at $x = a$, $y = h$. This field is matched to the solutions within the conductors as given in Appendix IV. In summary Appendix III and IV and the continuation condition give

$$H_x(x, y) = \begin{cases} H_o \frac{\sum Q_n C_n \sinh Q_n x \sin Q_n y}{\sum Q_n C_n} & 0 < x < a \\ \text{Neglected} & a < x < b+h \end{cases} \quad (7)$$

$$H_y(x, y) = \begin{cases} H_o \frac{\sum Q_n C_n \cosh Q_n x \cos Q_n y}{\sum Q_n C_n} & 0 < x < a \\ A_1 \sinh P(x-a) + B_1 \cosh P(x-a) & a < x < a+c \\ A_2 \sinh P(x-a-c) + B_2 \cosh P(x-a-c) & a+c < x < a+2c \\ \text{etc.}, & \end{cases} \quad (8)$$

where

$$P^2 = 4\pi\sigma_c j\omega, \quad (\text{emu}) \quad (9)$$

$$Q_n \tan Q_n h = 4\pi j\omega s, \quad (\text{emu}) \quad (10)$$

$$A_n \sinh P_c = -\frac{4\pi I}{h} [n - (n-1) \cosh P_c] - B_1 (\cosh P_c - 1), \quad (11)$$

$$B_n = -\frac{4\pi I}{h} (n-1) + B_1, \quad (12)$$

$$B_1 = H_y(a, h) + 4\pi j\omega s U(a, h) \quad (13)$$

$$C_n \left(Q_n \cosh Q_n a + 4\pi j\omega s \sinh Q_n a \right) \cdot \left(1 + \frac{\sin 2Q_n h}{2Q_n h} \right) = \frac{1}{h} \cdot \frac{\sin Q_n h}{Q_n h}. \quad (14)$$

Appendix III gives B_1 in terms of H_o , Q_n , and C_n .

In Eqs. (7-14) σ_c is the conductivity of the copper conductors, c is the horizontal width of the conductor, and H_o is the central magnetic field.

The magnetic circuit equations may now be evaluated. For $x = a$, Eq. (6) gives

$$V(a,h) + 4\pi j\omega s \int_0^h U(a,y) dy + \frac{k+1}{\mu} \left[\ell - \frac{1}{2}(p-h) \left(1 - \frac{w}{b} \right) \right] B_o \\ - \frac{k+1}{\mu} (p-h) \left[\left(B_{n_1+1} + \dots + B_{n_2} \right) \frac{\sinh P_c}{Pb} + \left(A_{n_1+1} + \dots + A_{n_2} \right) \cdot \frac{\cosh P_c - 1}{Pb} \right] = 2\pi NI, \quad (15)$$

where the expression in V and U is evaluated in Appendix III and n_1 and n_2 are the integer parts of $(b-a)/c$ and $(b-a+h)/c$. For convenience

$$k = \frac{\lambda\delta}{2} \cdot \frac{\cosh \frac{\lambda\delta}{2} - 1}{\sinh \frac{\lambda\delta}{2}}. \quad (16)$$

The other circuit equation, Eq. (1), becomes

$$U(a,h) + \left(B_1 + \dots + B_{n_2} \right) \frac{\sinh P_c}{P} + \left(A_1 + \dots + A_{n_2} \right) \cdot \frac{\cosh P_c - 1}{P} = wB_o. \quad (17)$$

After using Eqs. (11-13) and rearranging, Eqs. (15) and (17) become

$$V(a,h) + 4\pi j\omega s \int_0^h U(a,y) dy \\ - \frac{(k+1)(p-h)(n_2-n_1)(\cosh P_c - 1)}{\mu Pb \sinh P_c} \cdot \left[H_Y(a,h) + 4\pi j\omega s U(a,h) \right] \\ + \frac{k+1}{\mu} \left[\ell - \frac{1}{2}(p-h) \left(1 - \frac{w}{h} \right) \right] B_o = 2\pi I \left[N - \frac{(k+1)(p-h)(n_2^2 - n_1^2)(\cosh P_c - 1)}{\mu h Pb \sinh P_c} \right], \quad (18)$$

and

$$U(a,h) + 2n_2 \frac{(\cosh P_c - 1)}{P \sinh P_c} \left[H_y(a,h) + 4\pi j \omega s U(a,h) \right] \\ - wB_o = 4\pi I n_2^2 \frac{(\cosh P_c - 1)}{P h \sinh P_c} . \quad (19)$$

Appendix III relates the expressions in U , V , and H_y to H_o . Thus Eqs. (18) and (19) provide two linear equations which may be solved simultaneously for H_o and B_o in terms of I . Thus

$$H_o = TI, \quad (20)$$

where T , the transfer function, is obtained by eliminating B_o from Eqs. (18) and (19). In addition, the sextupole term introduced by the vacuum chamber may be found by differentiating Eq. (8) twice. Thus, using Eq. (20)

$$H_o'' = T \frac{\sum Q_n^3 C_n}{\sum Q_n C_n} I. \quad (21)$$

AC IMPEDANCE OF COIL

The inductance of the windings may be found by solving Eqs. (18) and (19) for B_o and using it to construct the flux linkage per unit current. Thus

$$L = \frac{2NwB_o}{I} \text{ (Magnet Length). (emu)} \quad (22)$$

The ac resistance of the conductors is found by finding the power loss of series connected conductors in a deep slot. For the main-ring magnets it seems reasonable to calculate this loss

assuming that the conductors are paired by twos in the layers of a deep slot. This calculation follows the reasoning of Appendix IV. See FN-111 for more detail. The conductor height is taken to be the average height of the inner and outer conductor heights. If the result of this calculation yields the resistance R , then the ac impedance of the magnet is

$$Z = R + j\omega L. \quad (25)$$

The inductance, of course, will have an imaginary part and contribute to the actual resistance seen between the coil terminals.

NUMERICAL RESULTS

The relations necessary to solve Eqs. (18) and (19) have been coded for the CDC 6600 in a program HITRANS which yields basically H_o/I and B_o/I for various frequencies and assumed permeabilities. The results are almost independent of the permeability which attests to the fact that the effects of eddy currents in the conductors and the vacuum chamber dominate over the eddy current effects in the magnet laminations. A reasonable choice of permeability might be the value giving the observed AMPFAC. If $T(0)$ designates the transfer function for dc, then

$$\text{AMPFAC} = \frac{2\pi N}{hT(0)}. \quad (26)$$

A second transfer function is produced from the T of Eq. (22) by noting that every magnet coil is paralleled by a 10-ohm resistor. Thus the effective transfer function TE is

$$TE = \frac{10}{10+z} \cdot T \quad (27)$$

Finally one should account for the capacitance of the coil to the yoke. The current passing into the capacitance is determined by the voltage to ground developed when the magnets are all connected in series and to the appropriate power supplies. A rough estimate of this effect using 12 power supplies and all identical magnets assuming .065 μ F for each magnet shows that this effect on the transfer function may be neglected below 10,000 Hz.

The attached computer output gives the transfer functions and ac impedances for the B1 and B2 magnets. The net bending for 378 B1 plus 396 B2 magnets is also given. A permeability of 3000 has been chosen since this gives approximately the observed AMPFAC. These numerical results are depicted graphically in Figs. (4-8).

ADDITIONAL CONSIDERATIONS

No account has been taken of hysteresis effects in the iron. This is considered justifiable if one has apriori knowledge that a frequency synthesis produces a monotonically varying function of time. If, however, one is interested in the response to a ripple frequency that might be present in the power supply, one should take into account the resistance added to the ac impedance by this power loss. The effect probably is small since the resistance contribution from the vacuum chamber is larger than that of the eddy currents in the laminations.

Finally, one should recognize that the approximations inherent in the use of an equivalent magnetic circuit and in a deep slot ac resistance calculation lead to uncertainties in all the above estimates. Perhaps the results are accurate to about 30 percent.

ACKNOWLEDGEMENTS

Information regarding appropriate physical constants such as conductivity of the laminations and the vacuum chamber was provided by R. Yamada. The coil-to-core capacitance was obtained from an October 15, 1971 memo to P. J. Reardon from Q. A. Kerns. Finally, thanks are due J. E. Griffin who provided the preliminary results of his measurements of the transfer function on the Bl magnet. The calculations on the Bl magnets are in substantial agreement with his data.

APPENDIX I
EDDY CURRENTS IN MAGNET LAMINATION

Figure 2 gives more detail of the infinite lamination on which the eddy current calculation will be based. If x designates the coordinate orthogonal to y and z as shown in Figure 2, then only B_x is needed and is governed by

$$\frac{\partial^2 B_x}{\partial z^2} - 4\pi\mu\sigma j\omega B_x = 0. \quad (\text{emu}) \quad (1)$$

Letting

$$\lambda^2 \equiv 4\pi\mu\sigma j\omega, \quad (2)$$

one has

$$B_x = \mu H \frac{\cosh \lambda z}{\cosh \frac{\lambda \delta}{2}}, \quad (3)$$

where μ is the permeability of the iron, σ the conductivity of the iron, and δ the lamination thickness.

The only value of B_x that can be used in the equivalent magnetic circuit analysis is the average value. From Eq. (3) one has for the average flux density

$$B = \frac{2\mu H}{\lambda \delta} \tanh \frac{\lambda \delta}{2}. \quad (4)$$

Figure 3 indicates the manner in which the infinite slab calculations are to be utilized for laminations of finite extent. In particular, the net current flowing along the edge of the lamination is assumed to be that current flowing vertically in one half of the infinite lamination. Thus the current per unit length is

$$4\pi i_I = H - H(0) = H \left(1 - \frac{1}{\cosh \lambda \frac{\delta}{2}} \right). \quad (\text{emu}) \quad (5)$$

Eliminating H between Eqs. (4) and (5) one arrives at

$$I_I = \frac{\lambda \delta}{8\pi\mu} \cdot \frac{\cosh \lambda \frac{\delta}{2} - 1}{\sin \lambda \frac{\delta}{2}} B. \quad (\text{emu}) \quad (6)$$

APPENDIX II
CURRENT FLOW IN THIN SHEETS

Figures 1c and 1d indicate the spatial relationships for the present calculation. The only assumption made is that the conducting sheet is sufficiently thin that the induced electric field does not vary throughout its thickness. For the vacuum chamber wall thickness of interest this means that the frequencies must be less than 100 kHz.

A gauge for which $\nabla \cdot \vec{A} = 0$ is used for the vector potential. Then $A_z(x, y)$ is adequate for the description of the fields. Thus

$$E_z = -j\omega A_z. \quad (\text{emu}) \quad (1)$$

Hence, the current density

$$J_z = \sigma E_z = -j\omega \sigma A_z, \quad (\text{emu})$$

where σ is the conductivity of the sheet. Hence, if i_c designates the current flowing in the sheet per cm and d is the thickness one has

$$i_c = J_z d = -j\omega \sigma d A_z. \quad (\text{emu}) \quad (3)$$

Letting $s = \sigma d$ the surface conductivity and

$$U(x, y) = -A_z(x, y) \quad (\text{emu}) \quad (4)$$

the flux function, one has

$$i_c(x, y) = j\omega s U(x, y). \quad (\text{emu}) \quad (5)$$

APPENDIX III
EDDY CURRENT FIELDS FROM RECTANGULAR CHAMBER
IN IDEAL DIPOLE MAGNET

An idealized calculation is made of the gap field in Fig.

1. The conductors are replaced by a sheet current I placed against the side wall of a window frame magnet of aperture $2a$ and gap $2h$. Permeability of iron is assumed infinite. In order to utilize this calculation in the main text, the current I is expressed in terms of the central field H_0 .

By superposition of elementary solutions of Laplace's equation one may choose

$$V(x,y) = 4\pi I \sum C_n \cosh Q_n x \sin Q_n y \quad (1)$$

for the scalar potential function and

$$U(x,y) = 4\pi I \sum C_n \sinh Q_n s \cos Q_n y \quad (2)$$

for the flux function. From Eq. (1) or Eq. (2) one has

$$H_x(x,y) = 4\pi I \sum Q_n C_n \sinh Q_n s \sin Q_n y \quad (3)$$

and

$$H_y(x,y) = 4\pi I \sum Q_n C_n \cosh Q_n x \cos Q_n y. \quad (4)$$

At $y = h$ the boundary condition is

$$H_x(x,h) = 4\pi i_C(x,h), \quad (5)$$

which from Appendix II gives

$$\sum C_n (Q_n \sin Q_n h - 4\pi j \omega s \cos Q_n h) \sinh Q_n x = 0. \quad (6)$$

Eq. (6) may be satisfied if Q_n is the solution

$$Q_n \tan Q_n h = 4\pi j \omega s. \quad (7)$$

At $x = a$ the boundary condition is

$$H_y(a, y) = \frac{2\pi I}{h} - 4\pi i_c(a, y), \quad (8)$$

which from Appendix I gives

$$\sum C_n \left(Q_n \cosh Q_n a + 4\pi j \omega s \sinh Q_n a \right) \cos Q_n y = \frac{1}{2h}. \quad (9)$$

The functions $\cos Q_n y$ form an orthogonal set since the Q_n satisfy Eq. (7). Therefore,

$$C_n \left(Q_n \cosh Q_n a + 4\pi j \omega s \sinh Q_n a \right) \left(1 + \frac{\sin 2Q_n h}{2Q_n h} \right) = \frac{1}{h} \cdot \frac{\sin Q_n h}{Q_n h}. \quad (10)$$

This expression for C_n formally completes the solution. One desires, however, to eliminate the current I by expressing it in terms of the central field. Thus, from Eq. (4)

$$H_o = 4\pi I \sum Q_n C_n. \quad (11)$$

In the main text it is shown that the following expressions are needed.

$$V(a, h) + 4\pi j \omega s \int_0^h U(a, y) dy = H_o \frac{\sum \left(\frac{\sin Q_n h}{Q_n h} \right)^2}{\sum \left(1 + \frac{\sin 2Q_n h}{2Q_n h} \right)}, \quad (12)$$

and

$$H_y(a, h) + 4\pi j \omega s U(a, h) = H_o \frac{\sum \frac{1}{1 + \frac{\sin 2Q_n h}{2Q_n h}}}{\sum h Q_n C_n}, \quad (13)$$

and

$$U(a,h) = H_0 \frac{\sum C_n \sinh Q_n a \cos Q_n h}{\sum Q_n C_n} . \quad (14)$$

Thus given Q_n as the solution of Eq. (7) and C_n from Eq. (10) the desired expressions are seen to be expressed in terms of H_0 the central field.

APPENDIX IV
FIELD IN DIPOLE MAGNET WITHIN CONDUCTORS IN GAP

An ideal situation is envisaged in which the magnet poles have infinite permeability, zero conductivity, and extend to infinity. Although easily modified for other cases, it is further assumed that only one layer of conductors exists between the median plane and the pole.

If the conductors are counted with the index n , $n = 1$ being the conductor beginning at the edge of the vacuum chamber (removed), then

$$H_{yn} = A_n \sinh Px + B_n \cosh Px, \quad (1)$$

where $x = 0$ at the left hand edge of each conductor of the right hand coil. Reasoning similar to that of Appendix I gives

$$P^2 = 4\pi j\omega\sigma, \quad (2)$$

where σ is the conductivity of the copper. Further, let c be the horizontal width of each conductor.

Continuity of H_y between conductors gives

$$H_{y,n+1}(0) = H_{y,n}(c) \quad (3)$$

or

$$B_{n+1} = A_n \sinh P_c + B_n \cosh P_c. \quad (4)$$

The ampere integral around the n th conductor gives

$$H_{yn}(0) - H_{yn}(c) = \frac{4\pi I}{h}, \quad (\text{emu}) \quad (5)$$

or

$$B_n - A_n \sinh P_c - B_n \cosh P_c = \frac{4\pi I}{h}. \quad (\text{emu}) \quad (6)$$

Equations (4) and (6) may be solved in terms of B_1 which in turn is the magnetic field in the aperture at the beginning of the conductors. Thus

$$A_n \sinh P_c = -\frac{4\pi I}{h} [n - (n-1) \cosh P_c] - (\cosh P_c - 1) B_1 \quad (7)$$

and

$$B_n = -\frac{4\pi I}{h} (n-1) + B_1. \quad (8)$$

Of course, B_1 would, in turn be related to I by a simple ampere integral around all the conductors. The intention, however, is to utilize the magnetic fields within the conductor as one component in a magnetic circuit. Hence B_1 and I are intentionally separated.

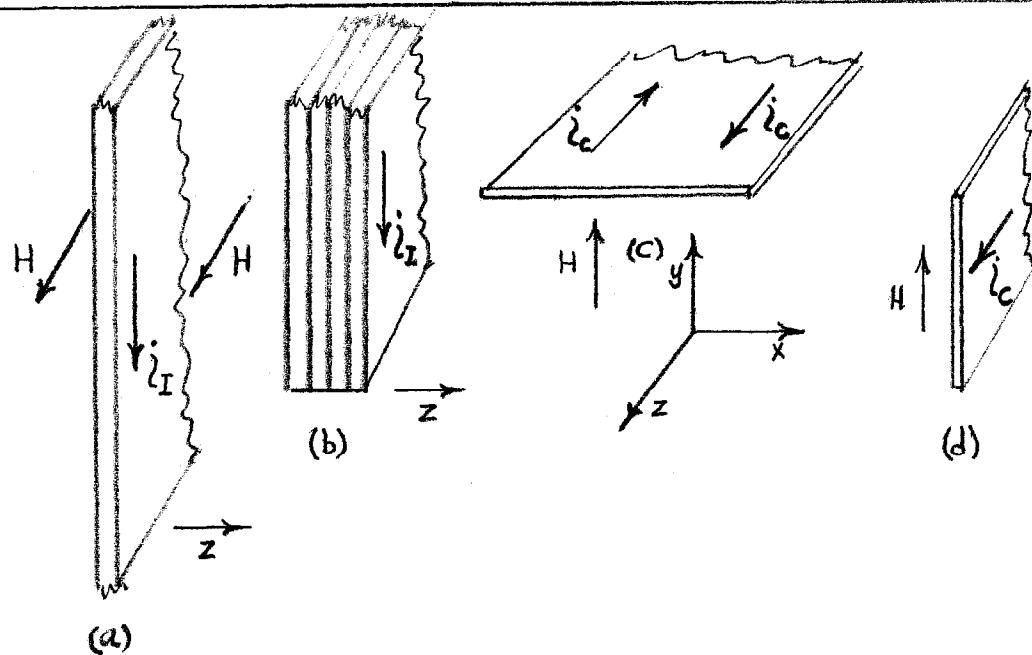
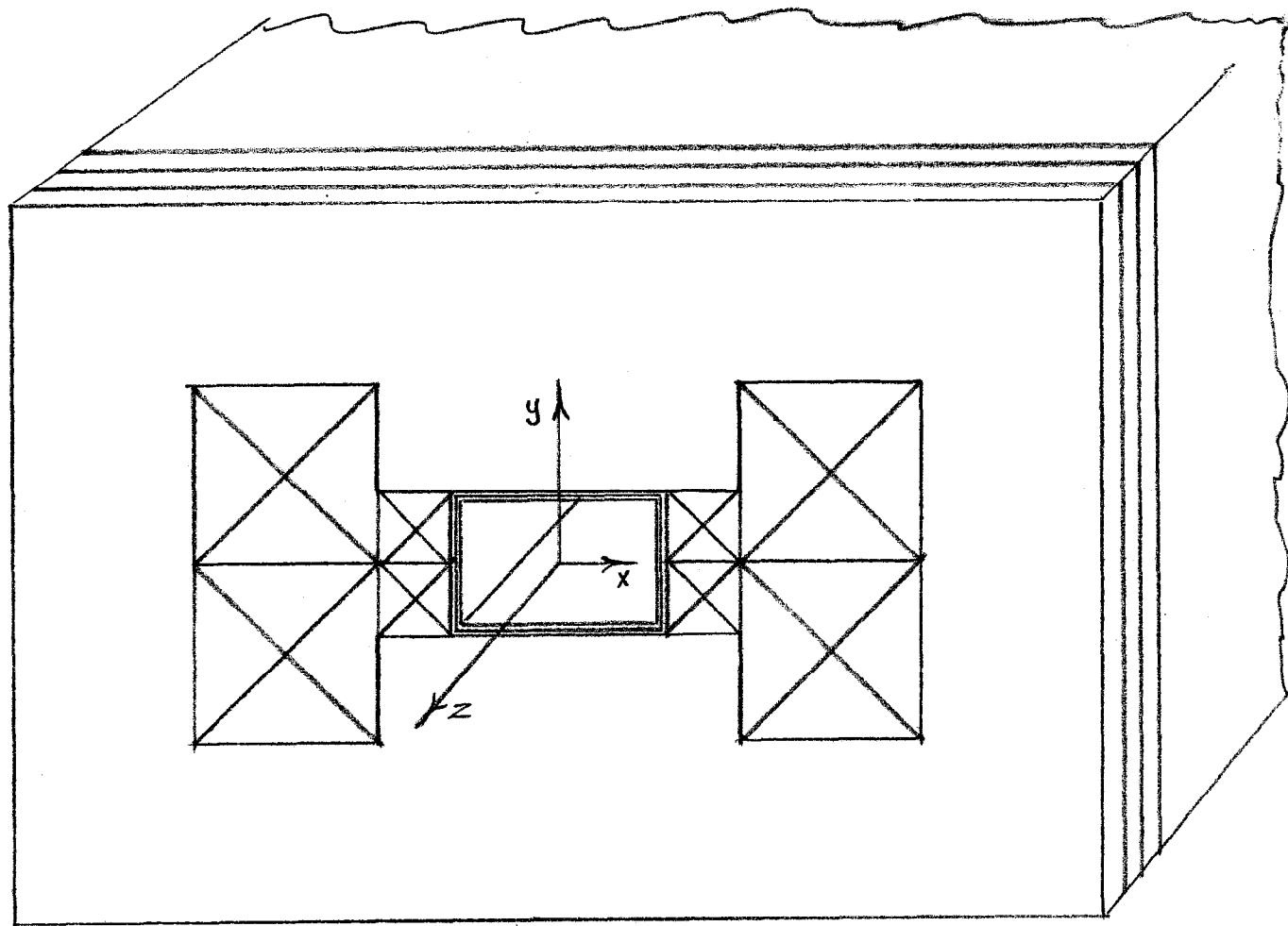


Fig. 1 MAGNET CROSS SECTION AND DETAILS

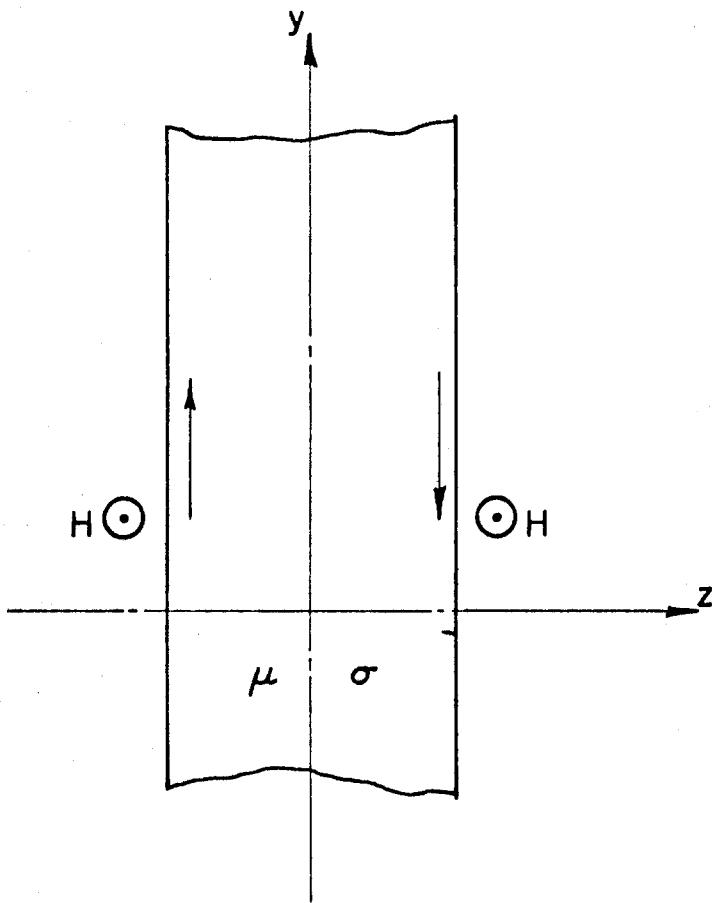


FIG. 2 INFINITE SLAB LAMINATION -
EDGE VIEW. MAGNETIC FIELD IS
DIRECTED UP OUT OF PAPER

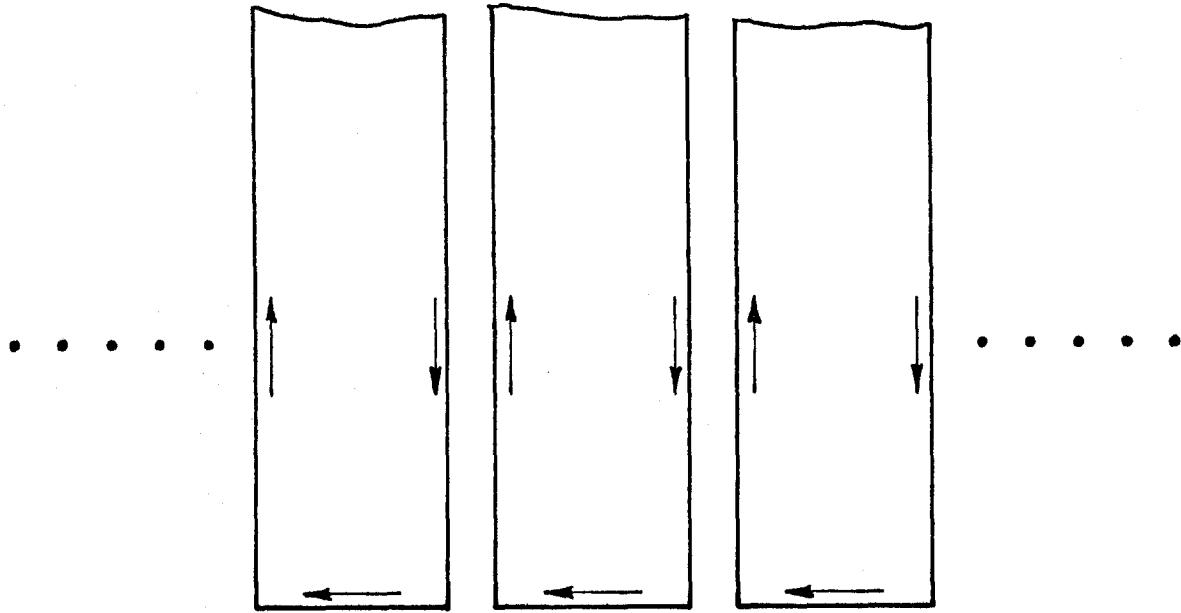
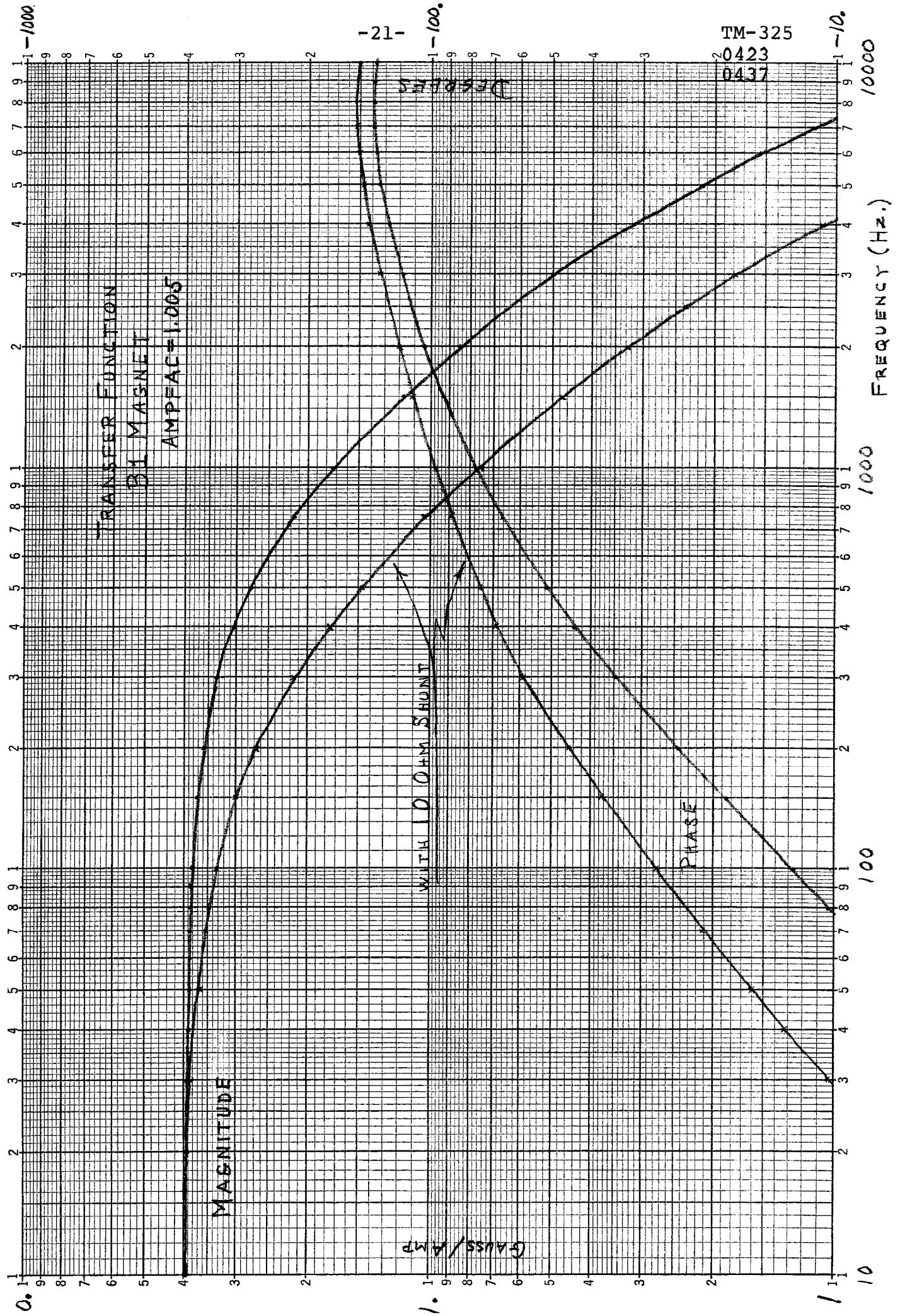


FIG. 3 SEMI INFINITE SLAB LAMINATION
EDGE VIEW



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FREQUENCY (Hz.)

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IMPEDANCE OF BI-MAGNET COIL

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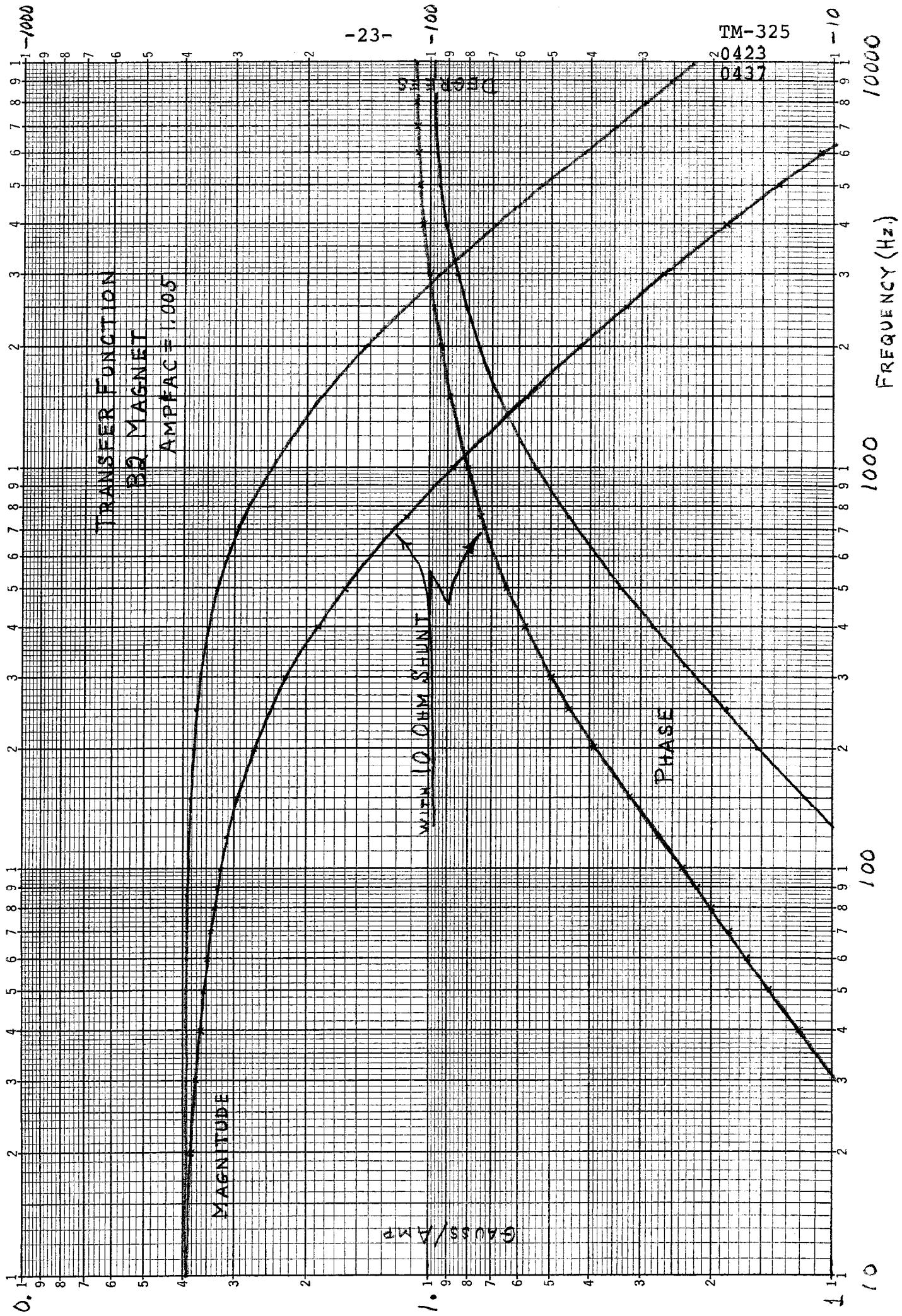
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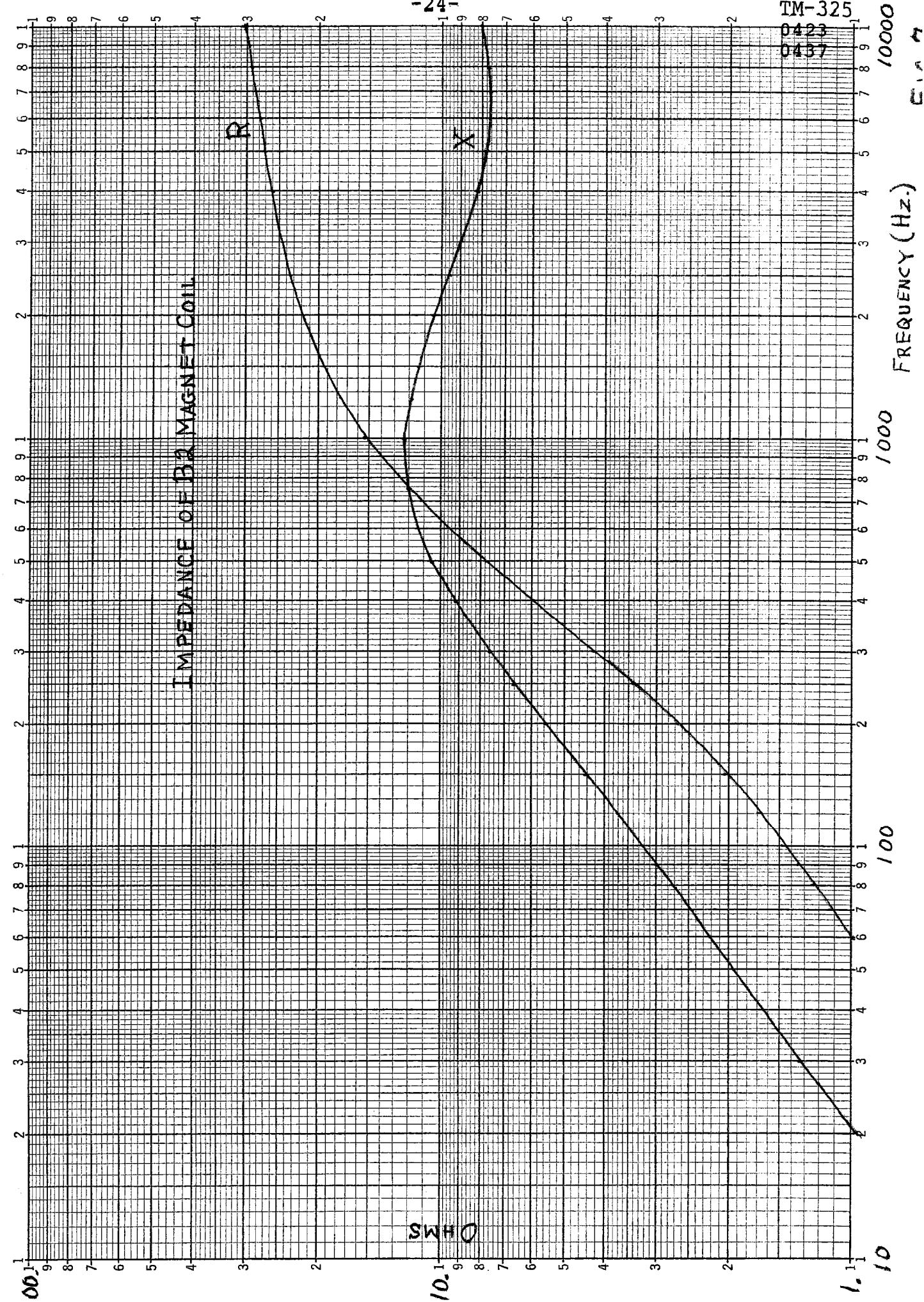
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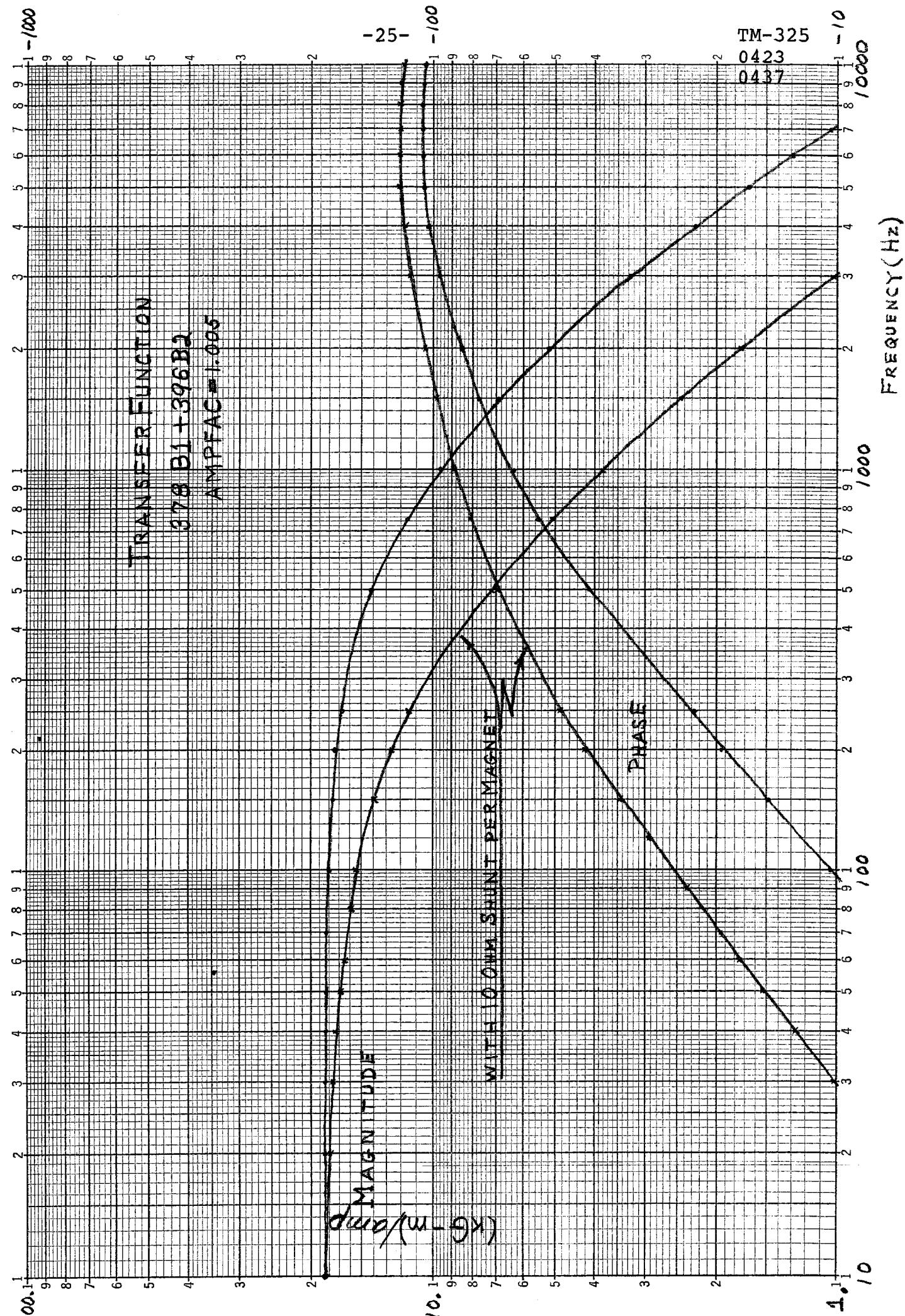
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TRANSFER FUNCTION BETWEEN FIELD AND CURRENT IN MAIN RING BENDING MAGNET(B1)

GAP(IN)	= 1.500 APER(IN)	= 5.000 POLE WIDTH(IN)	= 8.500 YOKE WIDTH(IN)	= 25.250
YOKE HEIGHT(IN)	= 14.250 YOKE THICKNESS(IN)	= 5.000 LAMINATION THICKNESS(IN)	= .0015 VAC. CHAMB. THICK.(IN)	= .050
IRON REST.(MUOHHM-CM)	= 12.000 VAC. CH. REST.(MUOHHM-CM)	= 75.500 PERMABILITY OF IRON	= 3000.0 AMPFAC	= 1.0056
DC INDUCTANCE(HY)	= .0041 COIL RESIST.(MUOHHM-IN)	= .772 COIL CORNER RADIUS(IN)	= .0625 MAGNET LENGTH(IN)	= 23.00
NO. TURNS IN INNER COIL	= 4 INNER COIL WIDTH(IN)	= 1.113 INNER COIL HEIGHT(IN)	= .670 INNER COIL HOLEDIAHM.(IN)	= .340
NO. TURNS IN OUTER COIL	= 8 OUTER COIL WIDTH(IN)	= 1.096 OUTER COIL HEIGHT(IN)	= .922 OUTER COIL HOLEDIAHM.(IN)	= .340

FRQ (HZ)	MAGNET ALONE		MAGNET WITH 10 OHMS	
	TRANSFER FCT. (GAUSS/AMP) (DEGREES)	AC IMPEDANCE (OHMS)	TRANSFER FCT. (GAUSS/AMP) (DEGREES)	AC IMPEDANCE (OHMS)
0.0000	3.9753	0.0000	3.9336	0.0000
5.0000	3.9353	-7.195	3.9297	-14.822
10.0000	3.8373	-1.4356	3.9183	-3.6276
15.0000	3.9327	-6.1462	3.9050	-5.001
20.0000	3.9259	-2.8484	3.8756	-7.1270
25.0000	3.9238	-3.5407	3.8462	-8.7990
30.0000	3.9149	-4.2224	3.8129	-10.4105
35.0000	3.9075	-4.9331	3.7768	-11.9591
40.0000	3.9016	-5.5533	3.7388	-13.4455
45.0000	3.8944	-6.2036	3.6997	-14.8723
50.0000	3.8871	-6.8451	3.6601	-16.2434
55.0000	3.8795	-7.4760	3.6204	-17.5635
60.0000	3.8719	-8.1058	3.5810	-18.8376
65.0000	3.8642	-8.7271	3.5420	-20.0704
70.0000	3.8564	-9.3435	3.5036	-21.2665
75.0000	3.8485	-9.9552	3.4658	-22.4297
80.0000	3.8406	-10.5640	3.4287	-23.5638
85.0000	3.8325	-11.1709	3.3922	-24.6715
90.0000	3.8244	-11.7742	3.3563	-25.7556
95.0000	3.8151	-12.3753	3.3210	-26.8180
100.0000	3.8077	-12.9743	3.2862	-27.8605
105.0000	3.7991	-13.5714	3.2519	-28.8945
110.0000	3.7904	-14.1666	3.2180	-29.8312
115.0000	3.7814	-14.7500	3.1845	-30.8813
120.0000	3.7723	-15.3514	3.1514	-31.8557
125.0000	3.7630	-15.9410	3.1186	-32.8150
130.0000	3.7575	-16.5200	3.0861	-33.7595
135.0000	3.7478	-17.1145	3.0539	-34.8097
140.0000	3.7332	-17.6982	3.0220	-35.6058
145.0000	3.7270	-18.2790	3.0004	-36.5082
150.0000	3.7135	-18.8592	3.0004	-37.3969
155.0000	3.7070	-19.4363	3.0004	-38.2722
160.0000	3.6922	-20.0111	3.0004	-39.1343
165.0000	3.6817	-20.5934	3.0005	-39.9833
170.0000	3.6731	-21.1533	3.0005	-40.8192
175.0000	3.6658	-21.7206	3.0005	-41.6424
180.0000	3.6472	-22.2952	3.0005	-42.4527
185.0000	3.6356	-22.8471	3.0005	-43.2905
190.0000	3.6237	-23.4063	3.0005	-44.0359
195.0000	3.6116	-23.9626	3.0005	-44.8089
200.0000	3.5997	-24.5150	3.0005	-45.5697

-261-

TM-325
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0437

TRANSFER FUNCTION BETWEEN FIELD AND CURRENT IN MAIN RING BENDING MAGNET (B2)

GAP(IN) = 2.00 APER(IN) = 4.000 POLE WIDTH(IN) = 7.500 YOLKE WIDTH(IN) = 25.250
 YOLKE HEIGHT(IN) = 14.250 YOLKE THICKNESS(IN) = 4.750 LAMINATION THICKNESS(IN) = .0615 VAC. CHAMB. THICK.(IN) = .050
 IRON REST.(MUOHM-CM) = 12.000 VAC. CH. REST.(MUOHM-CM) = 75.500 PERMEABILITY OF IRON = 3000.0 AMPFAC = 1.0045
 DC INDUCTANCE(HY) = .0022 COIL RESIST.(MUOHM-IN) = .772 COIL CORNER RADIUS(IN) = .0625 MAGNET LENGTH(IN) = 239.00
 NO. TURNS IN INNER COIL = 4 INNER COIL WIDTH(IN) = 1.096 INNER COIL HEIGHT(IN) = .922 INNER COIL HOLEDIAM.(IN) = .340
 NO. TURNS IN OUTER COIL = 12 OUTER COIL WIDTH(IN) = 1.096 OUTER COIL HEIGHT(IN) = .922 OUTER COIL HOLEDIAM.(IN) = .445

FREQ (HZ)	MAGNET ALONE		MAGNET WITH 10 OHMS	
	TRANSFER FCT. (GAUSS/AMP) (DEGREES)	AC IMPEDANCE (OHMS)	TRANSFER FCT. (GAUSS/AMP) (DEGREES)	AC IMPEDANCE (OHMS)
0.0000	3.9402	0.0000	3.9373	0.0000
5.0000	3.9397	-4.4340	3.9287	-1.9040
10.0000	3.9397	-4.8641	3.9044	-3.7416
15.0000	3.9369	-1.2972	3.8677	-5.4532
20.0000	3.9331	-1.7015	3.8234	-7.0446
25.0000	3.9299	-2.1056	3.7754	-8.852
30.0000	3.9263	-2.5031	3.7269	-9.7998
35.0000	3.9227	-2.9922	3.6798	-11.0104
40.0000	3.9191	-3.2751	3.6353	-12.1395
45.0000	3.9155	-3.6531	3.5936	-13.2071
50.0000	3.9121	-4.0273	3.5547	-14.2291
55.0000	3.9086	-4.395	3.5183	-15.2178
60.0000	3.9052	-4.7674	3.4840	-16.1819
65.0000	3.9019	-5.1346	3.4516	-17.1275
70.0000	3.8984	-5.5005	3.206	-18.0589
75.0000	3.8950	-5.8653	3.3907	-18.9767
80.0000	3.8915	-6.2293	3.3618	-19.8887
85.0000	3.8881	-6.5926	3.3335	-20.7900
90.0000	3.8846	-6.9554	3.3057	-21.6829
95.0000	3.8811	-7.3176	3.2784	-22.5677
100.0000	3.8774	-7.6793	3.2399	3.2513
105.0000	3.8737	-8.0405	3.3659	3.2244
110.0000	3.8699	-8.4015	3.4918	3.1977
115.0000	3.8661	-8.7619	3.6173	3.1710
120.0000	3.8621	-9.0217	3.7427	3.1444
125.0000	3.8581	-9.4815	3.8677	3.1178
130.0000	3.8542	-9.8405	3.9923	3.0912
135.0000	3.8497	-10.1771	4.1165	3.0646
140.0000	3.8453	-10.5571	4.2402	3.0381
145.0000	3.8409	-10.9146	4.3635	3.0115
150.0000	3.8363	-11.2714	4.4861	2.9850
155.0000	3.8318	-11.6277	4.6082	2.9585
160.0000	3.8273	-11.9934	4.7296	2.9321
165.0000	3.8229	-12.3393	4.8504	2.9057
170.0000	3.8179	-12.6926	4.9704	2.8793
175.0000	3.8119	-13.0462	5.0896	2.8531
180.0000	3.8067	-13.3993	5.2081	2.8269
185.0000	3.8014	-13.7517	5.3257	2.8008
190.0000	3.7953	-14.1022	5.4425	2.7749
195.0000	3.7904	-14.4525	5.5584	2.7491
200.0000	3.7843	-14.8022	5.6734	2.7234

TRANSFER FUNCTION FOR NET BENDING FROM 378 A1 PLUS 396 B2 MAGNETS

FREQ (HZ)	MAGNET ALONE			MAGNET WITH 10 OHMS		
	TRANSFER FCT. (KG-M)/AMP	AC IMPEDANCE (KOHMS)	DEGREES	TRANSFER FCT. (KG-M)/AMP	AC IMPEDANCE (KOHMS)	DEGREES
0.0000	18.5073	0.0000	.0051	0.0000	18.4915	0.0000
5.0000	18.5010	-5.733	.0144	.1747	18.4620	-1.8641
10.0000	18.4928	-1.1431	.0410	.3456	18.3772	-3.6858
15.0000	18.4798	-1.7064	.0823	.5027	18.2471	-5.4323
20.0000	18.4578	-2.2611	.1344	.6650	18.0844	-7.0351
25.0000	18.4425	-2.8052	.1936	.8111	17.9015	-8.6193
30.0000	18.4201	-3.3415	.2567	.9482	17.7084	-10.1015
35.0000	18.3960	-3.8676	.3212	1.0773	17.5122	-11.4799
40.0000	18.3708	-4.3952	.3855	1.1995	17.3175	-12.7365
45.0000	18.3449	-4.9053	.4485	1.3158	17.1269	-14.0324
50.0000	18.3145	-5.3992	.5098	1.4274	16.9416	-15.2276
55.0000	18.2918	-5.8971	.5692	1.5390	16.7621	-16.3802
60.0000	18.2649	-6.3935	.6266	1.6394	16.5983	-17.4971
65.0000	18.2372	-6.8904	.6822	1.7412	16.4199	-18.5838
70.0000	18.2175	-7.3863	.7363	1.8408	16.2562	-19.6446
75.0000	18.1979	-7.8507	.7889	1.9386	16.0968	-20.6330
80.0000	18.1551	-8.3323	.8403	2.0348	15.9411	-21.7016
85.0000	18.1260	-8.8110	.8907	2.1297	15.7886	-22.7026
90.0000	18.0982	-9.2809	.9404	2.2235	15.6367	-23.6873
95.0000	18.0690	-9.7652	.9895	2.3162	15.4911	-24.6571
100.0000	18.0393	-10.2412	1.0382	2.4081	15.3454	-25.6128
105.0000	18.0090	-10.7147	1.0867	2.4991	15.2013	-26.5551
110.0000	17.9781	-11.1970	1.1350	2.5693	15.0585	-27.4843
115.0000	17.9475	-11.6570	1.1833	2.6787	14.9169	-28.4008
120.0000	17.9142	-12.1275	1.2316	2.7674	14.7763	-29.3049
125.0000	17.8812	-12.5950	1.2802	2.8554	14.6366	-30.1965
130.0000	17.8475	-13.0626	1.3289	2.9427	14.4976	-31.0760
135.0000	17.8129	-13.5291	1.3783	3.0292	14.3594	-31.9432
140.0000	17.7777	-13.9920	1.4275	3.1150	14.2218	-32.7983
145.0000	17.7416	-14.4544	1.4773	3.2001	14.0850	-33.6412
150.0000	17.7049	-14.0152	1.5277	3.2845	13.9488	-34.4719
155.0000	17.6677	-15.3744	1.5784	3.3681	13.8132	-35.2346
160.0000	17.6288	-15.8310	1.6297	3.4509	13.6784	-36.0971
165.0000	17.5907	-16.2975	1.6815	3.5329	13.5443	-36.9915
170.0000	17.5493	-16.7414	1.7338	3.6141	13.4110	-37.6739
175.0000	17.5092	-17.1334	1.7866	3.6946	13.2714	-38.4442
180.0000	17.4673	-17.6435	1.8400	3.7741	13.1467	-39.2026
185.0000	17.4259	-18.0916	1.8939	3.8529	13.0159	-39.9492
190.0000	17.3831	-18.5377	1.9484	3.9378	12.8860	-40.6839
195.0000	17.3397	-19.0918	2.0033	4.0078	12.7570	-41.4069
200.0000	17.2955	-19.237	2.0588	4.0839	12.6291	-42.1184

TRANSFER FUNCTION BETWEEN FIELD AND CURRENT IN MAIN RING BENDING MAGNET (B1)

GAP(IN)	= 1.500	APER(IN)	= 5.000	POLF WIDTH(IN)	= 8.500	YODE WIDTH(IN)	= 25.250
YODE HEIGHT(IN)	= 14.250	YODE THICKNESS(IN)	= 5.000	LAMINATION THICKNESS(IN)	= .0615	VAC. CHAMB. THICK.(IN)	= .050
IRON REST.(MUOHM-CM)	= 12.000	VAC. CH. REST.(MUOHM-CM)	= 75.500	PERMFABILITY OF IRON	= 3000.0	AMPFAC	= 1.0356
DC INDUCTANCE(HY)	= .0061	COIL RESIST.(MUOHM-IN)	= .772	COIL CORNER RADIUS(IN)	= .0625	MAGNET LENGTH(IN)	= 239.00
NO. TURNS IN INNER COIL	= 4	INNER COIL WIDTH(IN)	= 1.113	INNER COIL HEIGHT(IN)	= .670	INNER COIL HOLEDIAM.(IN)	= .340
NO. TURNS IN OUTER COIL	= 8	OUTER COIL WIDTH(IN)	= 1.096	OUTER COIL HEIGHT(IN)	= .922	OUTER COIL HOLEDIAM.(IN)	= .340

FRQ (HZ)	MAGNET ALONE			MAGNET WITH 10 OHMS		
	TRANSFER FCT. (GAUSS/AMP)	(DEGREES)	AC IMPEDANCE (OHMS)	TRANSFER FCT. (GAUSS/AMP)	(DEGREES)	AC IMPEDANCE (OHMS)
0.0000	3.9359	0.0000	.0059	0.0000	3.9336	0.0000
250.0000	3.4625	-29.8794	3.3995	5.5922	2.3891	-52.5422
500.0000	2.7447	-51.6815	7.0994	7.4396	1.4721	-75.2218
750.0000	2.1425	-65.6290	9.7044	7.6969	1.0131	-88.0109
1000.0000	1.7075	-77.4273	11.2242	7.5732	.7579	-77.1205
1250.0000	1.3936	-85.7660	12.3838	7.4251	.5311	-104.1983
1500.0000	1.1605	-92.5770	13.2648	7.3207	.4760	-110.1430
1750.0000	.9320	-98.3463	13.9856	7.2580	.3920	-115.2989
2000.0000	.8415	-103.3550	14.6067	7.2225	.3783	-119.8462
2250.0000	.7284	-107.7731	15.1596	7.2017	.2785	-123.9001
2500.0000	.6358	-111.7094	15.6613	7.1865	.2387	-127.5270
2750.0000	.5588	-115.2375	16.1218	7.1717	.2064	-130.7812
3000.0000	.4940	-118.4101	16.5468	7.1544	.1798	-133.7033
3250.0000	.4390	-121.2552	16.9404	7.1332	.1576	-136.3259
3500.0000	.3920	-123.8370	17.3053	7.1080	.1390	-138.6766
3750.0000	.3514	-126.1476	17.6440	7.0792	.1232	-140.7791
4000.0000	.3163	-128.2103	17.3584	7.0476	.1098	-142.6542
4250.0000	.2847	-130.0703	18.2504	7.0141	.0982	-144.3201
4500.0000	.2529	-131.7170	18.5219	6.9797	.0892	-145.7933
4750.0000	.2353	-133.1730	18.7745	6.9453	.0796	-147.0886
5000.0000	.2145	-134.4543	19.0098	6.9116	.0720	-148.2193
5250.0000	.1962	-135.5705	19.2294	6.8793	.0654	-149.1978
5500.0000	.1800	-136.5330	19.4347	6.8490	.0596	-150.0354
5750.0000	.1655	-137.3542	19.6271	6.8210	.0545	-150.7424
6000.0000	.1526	-138.0436	19.8079	6.7958	.0499	-151.3286
6250.0000	.1410	-138.6096	19.9781	6.7736	.0459	-151.8030
6500.0000	.1307	-139.0616	20.1390	6.7545	.0423	-152.1742
6750.0000	.1214	-139.4003	20.2915	6.7387	.0391	-152.4502
7000.0000	.1120	-139.6576	20.4365	6.7260	.0363	-152.6385
7250.0000	.1044	-139.8173	20.5749	6.7166	.0337	-152.7463
7500.0000	.0966	-139.8947	20.7073	6.7104	.0314	-152.7804
7750.0000	.0924	-139.8959	20.8345	6.7073	.0293	-152.7472
8000.0000	.0880	-139.8301	20.9571	6.7071	.0274	-152.6527
8250.0000	.0817	-139.7011	21.0755	6.7097	.0257	-152.5328
8500.0000	.0771	-139.5155	21.1904	6.7151	.0242	-152.3028
8750.0000	.0728	-139.2702	21.3021	6.7229	.0228	-152.0579
9000.0000	.0680	-139.9973	21.4109	6.7332	.0215	-151.7729
9250.0000	.0654	-138.5748	21.5174	6.7457	.0203	-151.4522
9500.0000	.0621	-138.3165	21.6217	6.7602	.0192	-151.1003
9750.0000	.0591	-137.9267	21.7241	6.7766	.0182	-150.7209
10000.0000	.0564	-137.5095	21.8249	6.7948	.0173	-150.3177

TRANSFER FUNCTION BETWEEN FIELD AND CURRENT IN MAIN PING BENDING MAGNET (92)

GAP(IN) = 2.000 APER(IN) = 4.000 POLE WIDTH(IN) = 7.500 YOKE WIDTH(IN) = 25.250
 YOKE HEIGHT(IN) = 14.250 YOKE THICKNESS(IN) = 4.750 LAMINATION THICKNESS(IN) = .0615 VAC. CHAMB. THICK.(IN) = .050
 IRON REST.(MUOHM-CM) = 12.000 VAC. CH. REST.(MUOHM-CM) = 75.500 PERMEABILITY OF IRON = 3000.0 AMPFAC = 1.0345
 DC INDUCTANCE(HY) = .0082 COIL RESIST.(MUOHM-IN) = .772 COIL COPPER RADIUS(IN) = .0625 MAGNET LENGTH(IN) = 233.00
 NO. TURNS IN INNER COIL = 4 INNER COIL WIDTH(IN) = 1.096 INNER COIL HEIGHT(IN) = .922 INNER COIL HOLEDIAM.(IN) = .340
 NO. TURNS IN OUTER COIL = 12 OUTER COIL WIDTH(IN) = 1.096 OUTER COIL HEIGHT(HN) = .922 OUTER COIL HOLEDIAM.(IN) = .445

FREQ (HZ)	MAGNET ALONE		MAGNET WITH 10 OHMS	
	TRANSFER FCT. (GAUSS/AMP) (DEGREES)	AC IMPEDANCE (OHMS)	TRANSFER FCT. (GAUSS/AMP) (DEGREES)	AC IMPEDANCE (OHMS)
0.0000	2.9477	0.0000	3.9373	0.0000
250.0000	3.7223	-18.2458	3.4219	6.7683
500.0000	3.3097	-33.6216	7.7972	10.5530
750.0000	2.9495	-45.6253	11.7191	12.0001
1000.0000	2.4377	-54.7720	14.9636	12.0839
1250.0000	2.0990	-61.8124	17.3620	11.8452
1500.0000	1.8230	-67.3547	19.1327	11.3428
1750.0000	1.6003	-71.8234	20.4681	10.8258
2000.0000	1.4183	-75.5044	21.5040	10.3487
2250.0000	1.2677	-78.4504	22.3307	9.9270
2500.0000	1.1416	-81.2139	23.0075	9.5607
2750.0000	1.0349	-83.4678	23.5742	9.2448
3000.0000	.9437	-85.4194	24.0578	8.9731
3250.0000	.8643	-87.1185	24.4771	8.7395
3500.0000	.7963	-88.5030	24.8458	8.5389
3750.0000	.7357	-89.9020	25.1738	8.3669
4000.0000	.6934	-91.0417	25.687	8.2198
4250.0000	.6565	-92.0393	25.7363	8.1947
4500.0000	.6347	-92.9121	25.9812	7.9889
4750.0000	.5578	-93.6741	26.2072	7.9004
5000.0000	.5237	-94.3376	26.4174	7.8273
5250.0000	.4934	-94.9131	26.6143	7.7680
5500.0000	.4661	-95.4101	26.8000	7.7212
5750.0000	.4412	-95.8359	26.9763	7.6855
6000.0000	.4186	-96.2011	27.1447	7.6599
6250.0000	.3979	-96.5024	27.3066	7.6433
6500.0000	.3790	-96.7670	27.4629	7.6349
6750.0000	.3616	-96.9927	27.6147	7.6337
7000.0000	.3457	-97.1557	27.7627	7.6391
7250.0000	.3317	-97.2955	27.9076	7.6503
7500.0000	.3174	-97.4053	28.0500	7.6666
7750.0000	.3040	-97.4850	28.1903	7.6874
8000.0000	.2931	-97.5442	28.3290	7.7124
8250.0000	.2822	-97.5905	28.4663	7.7408
8500.0000	.2721	-97.5982	28.6026	7.7724
8750.0000	.2627	-97.5995	28.7381	7.8067
9000.0000	.2539	-97.5970	28.8729	7.8433
9250.0000	.2455	-97.5621	29.0073	7.8819
9500.0000	.2379	-97.5287	29.1414	7.9222
9750.0000	.2305	-97.4822	29.2752	7.8639
10000.0000	.2239	-97.4299	29.4089	8.0068

-30-

TM-325
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TRANSFER FUNCTION FOR NET BENDING FROM 378 B1 PLUS 396 B2 MAGNETS

FREQ (HZ)	MAGNET ALONE			MAGNET WITH 10 OHMS		
	TRANSFER FCT. (KG-M)/AMP	(DEGREES)	AC IMPEDANCE (KOHMS)	TRANSFER FCT. (KG-M)/AMP	(DEGREES)	AC IMPEDANCE (KOHMS)
0.0000	18.5038	0.0000	.0051	0.0000	18.4915	0.0000
250.0000	1F.9220	-23.7207	2.6401	4.7941	11.4123	-48.6243
500.0000	14.0779	-41.5937	5.7713	6.9912	7.1907	-69.4171
750.0000	11.5727	-54.3845	8.3090	7.6615	5.0506	-90.7281
1000.0000	9.5956	-63.8197	10.1683	7.6875	3.8112	-88.2017
1250.0000	8.0710	-71.0595	11.5564	7.4974	3.0077	-93.7072
1500.0000	6.8857	-76.8405	12.5906	7.2590	2.4518	-98.0972
1750.0000	5.9489	-81.5615	13.3919	7.0305	2.0457	-101.7311
2000.0000	5.1956	-85.5025	14.0369	6.8282	1.7372	-104.8025
2250.0000	4.5793	-88.8477	14.5733	6.6533	1.4958	-107.4284
2500.0000	4.0694	-91.6958	15.0309	6.5025	1.3025	-109.6863
2750.0000	3.6411	-94.1526	15.4294	6.3719	1.1450	-111.6317
3000.0000	3.2770	-95.2733	15.7816	6.2577	1.0148	-113.3072
3250.0000	2.9673	-98.1053	16.0964	6.1572	.9058	-114.7467
3500.0000	2.6994	-99.6°F2	16.3803	6.0682	.8137	-115.9783
3750.0000	2.4650	-101.0463	16.6383	5.9892	.7352	-117.0262
4000.0000	2.2640	-102.2113	16.8739	5.9130	.6677	-117.9109
4250.0000	2.0859	-103.2029	17.0902	5.8568	.6093	-118.6509
4500.0000	1.9298	-104.0302	17.2898	5.8019	.5585	-119.2623
4750.0000	1.7897	-104.7303	17.4748	5.7539	.5143	-119.7596
5000.0000	1.6651	-105.3159	17.6470	5.7122	.4749	-120.1557
5250.0000	1.5557	-105.7932	17.8080	5.6765	.4404	-120.4623
5500.0000	1.4570	-106.1533	17.9591	5.6465	.4097	-120.8900
5750.0000	1.3683	-106.4371	18.1017	5.6218	.3824	-120.8484
6000.0000	1.2883	-106.6446	18.2367	5.6021	.3579	-120.9459
6250.0000	1.2151	-106.7949	18.3651	5.5872	.3360	-120.9905
6500.0000	1.1506	-106.9852	18.4879	5.5756	.3162	-120.9892
6750.0000	1.0912	-106.8860	18.6056	5.5702	.2983	-120.9481
7000.0000	1.0370	-106.9930	18.7190	5.5675	.2821	-120.8730
7250.0000	.9875	-106.8220	18.8287	5.5684	.2674	-120.7689
7500.0000	.9427	-106.7306	18.9352	5.5725	.2539	-120.6404
7750.0000	.9077	-106.6239	19.0388	5.5796	.2416	-120.4914
8000.0000	.8624	-106.4940	19.1401	5.5834	.2304	-120.3256
8250.0000	.8272	-106.3239	19.2392	5.6016	.2200	-120.1461
8500.0000	.7946	-106.1470	19.3366	5.6162	.2104	-119.9556
8750.0000	.7644	-105.9564	19.4325	5.6327	.2016	-119.7566
9000.0000	.7354	-105.7547	19.5270	5.6511	.1935	-119.5511
9250.0000	.7104	-105.5443	19.6205	5.6711	.1859	-119.3411
9500.0000	.6861	-105.3273	19.7130	5.6925	.1788	-119.1279
9750.0000	.6635	-105.1053	19.8047	5.7153	.1723	-118.9131
10000.0000	.6421	-104.8801	19.8957	5.7391	.1661	-118.6978

-31-

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